

Relational Interpretation of Concurrency

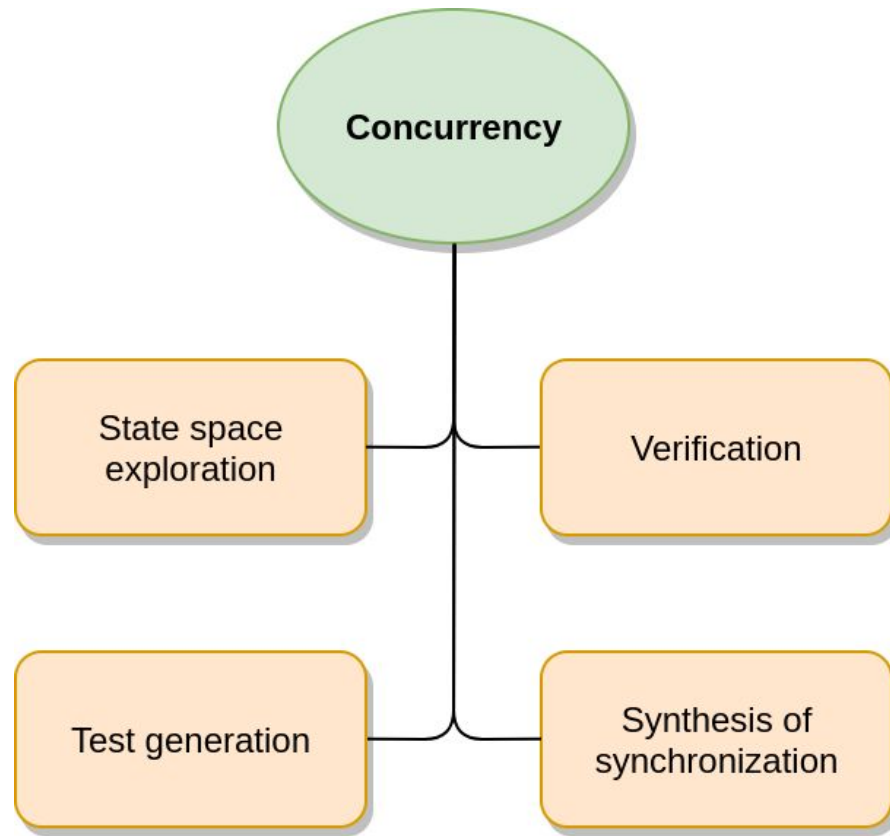
Evgenii Moiseenko

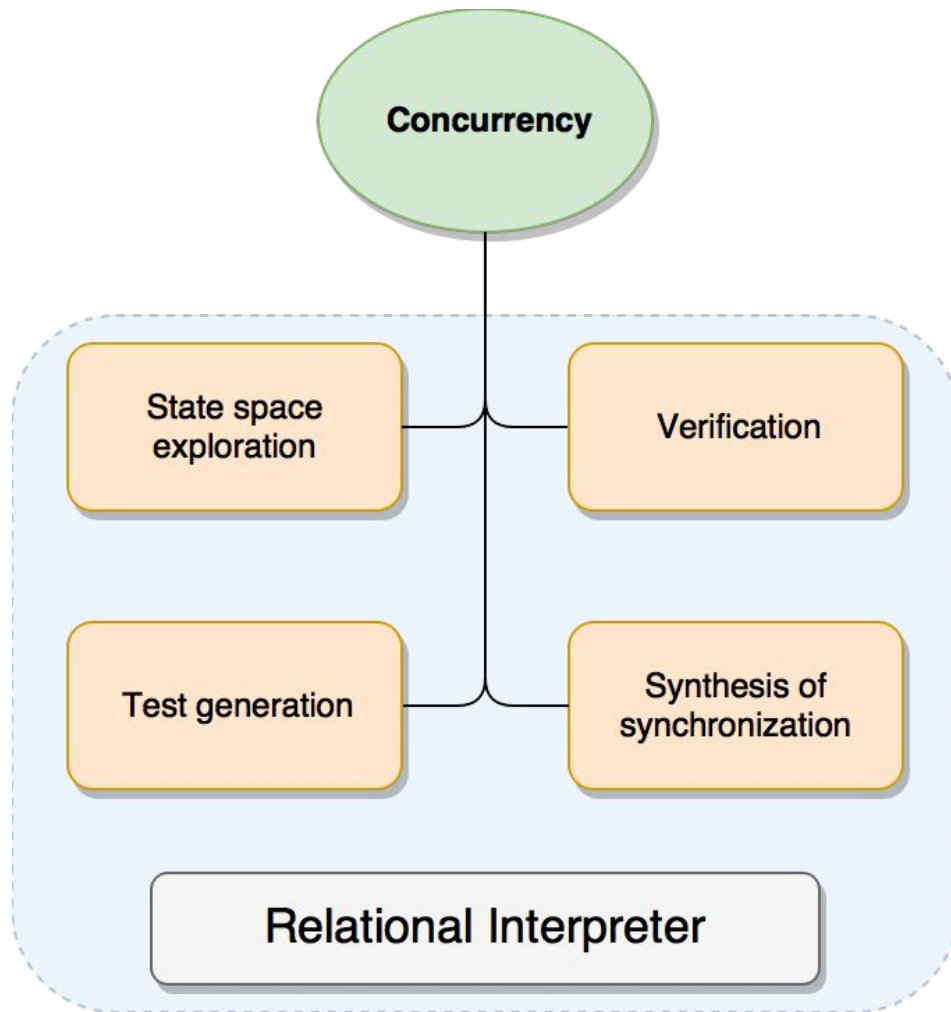
Anton Podkopaev



Plan

- Relational Programming
- Relational Interpreter
- Relational Interpreter for Concurrency





Functional Programming

`[3; 2; 1]` $\xrightarrow{\text{sort}}$ `[1; 2; 3]`

Relational Programming

```
[1; 2; 3]
[1; 3; 2]
[2; 1; 3]
[2; 3; 1]
[3; 2; 1]
[3; 1; 2]
```

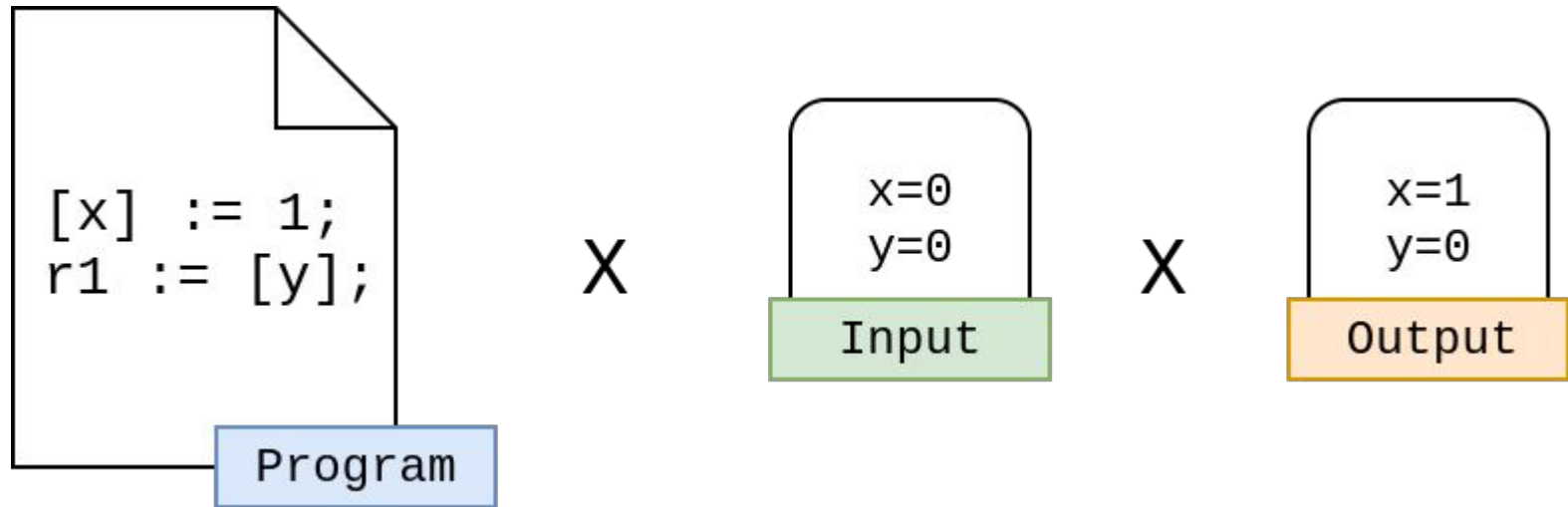
sort

[1; 2; 3]

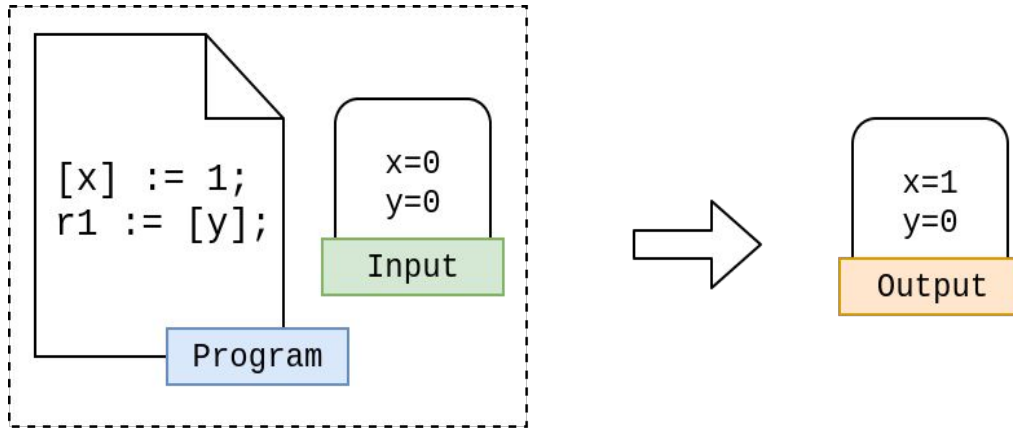
OCanren

- OCaml DSL for Relational Programming
 - Declarative specification of relations
 - Complete backtracking search

Relational Interpreter

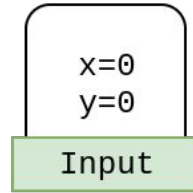
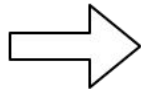
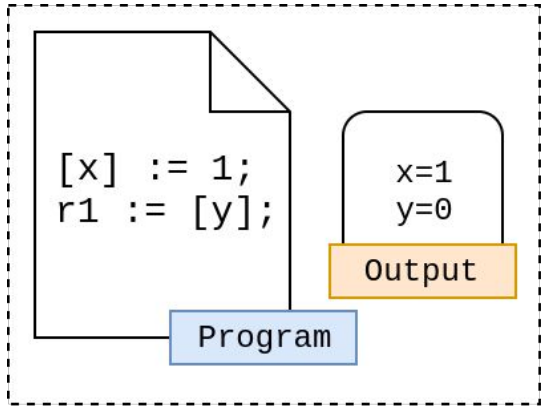


Relational Interpreter



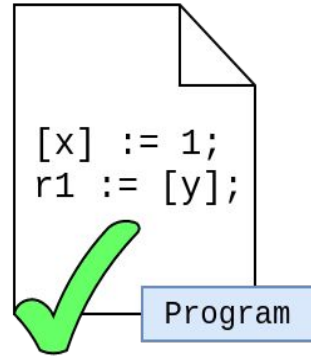
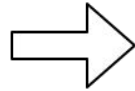
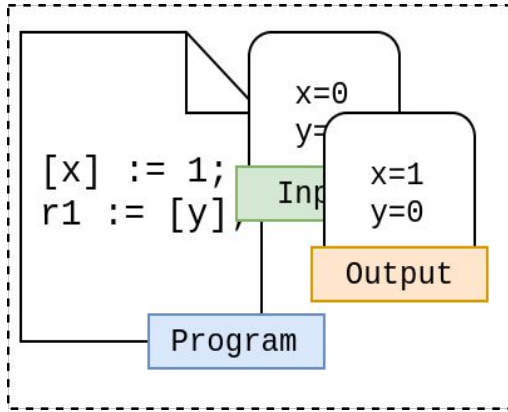
- Execution

Relational Interpreter



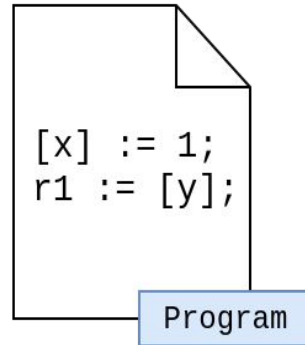
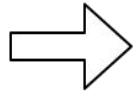
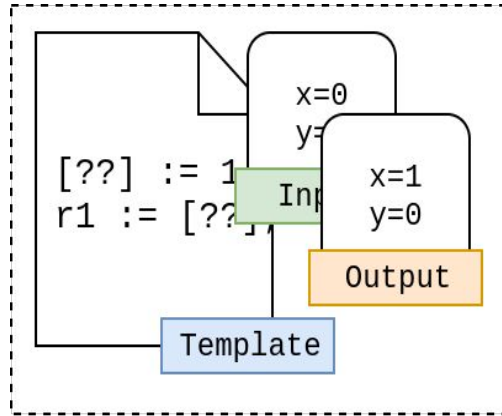
- Execution
- Test generation

Relational Interpreter



- Execution
- Test generation
- Verification

Relational Interpreter



- Execution
- Test generation
- Verification
- Synthesis

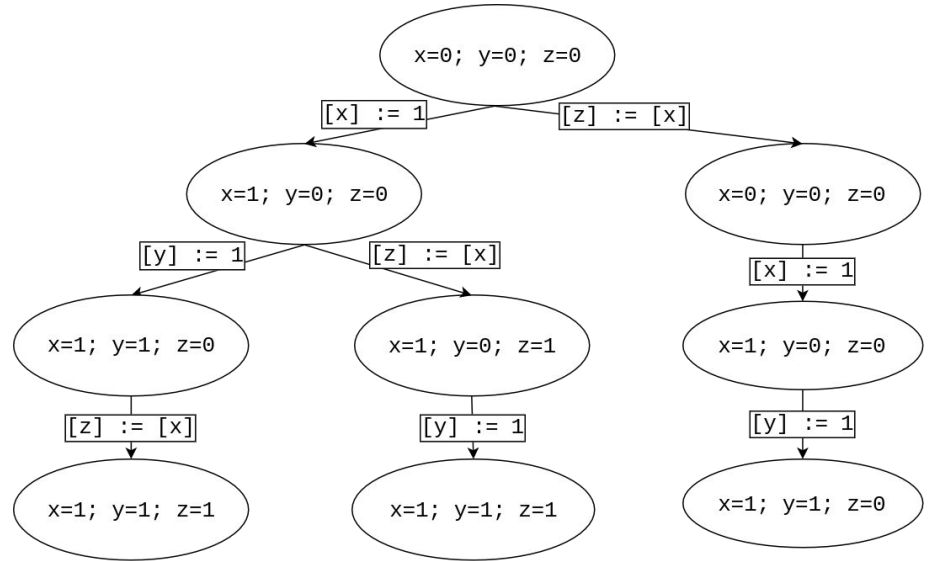
Results

- Relational Interpreter for Concurrency
 - Compact and declarative (~1.5K lines of code)
- Extension of OCanren
 - Tabling – memoization for relational programs
 - Efficient state space exploration
 - Constructive negation
 - Allows to express negative examples

Transition Labeled System

[x] := 1;
[y] := 1;

[z] := [x];



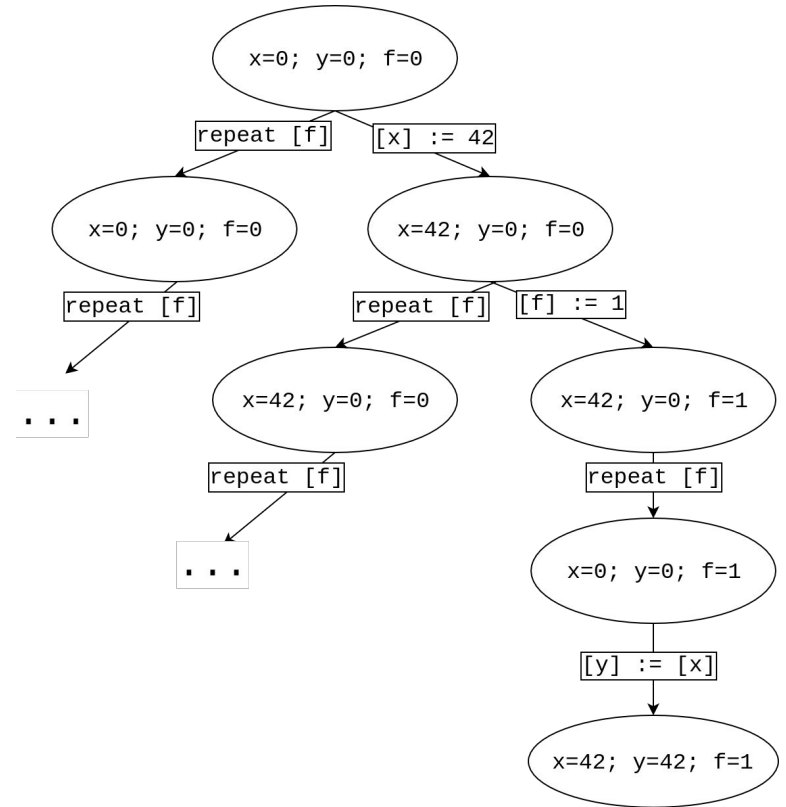
Memoization

```
[x] := 42;
```

```
[f] := 1;
```

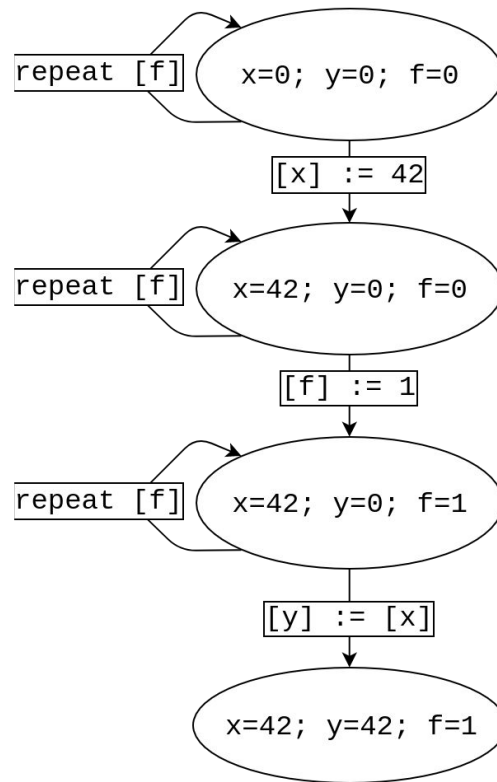
```
repeat [f];
```

```
[y] := [x];
```



Memoization

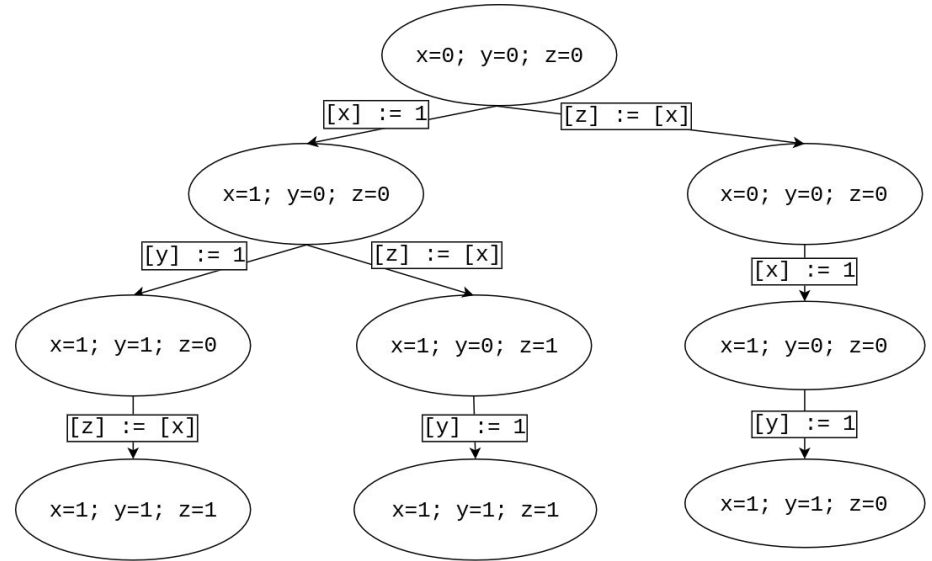
```
[x] := 42; | repeat [f];  
[f] := 1; | [y] := [x];
```



Angelic Execution

Input: $x=0; y=0; z=0$

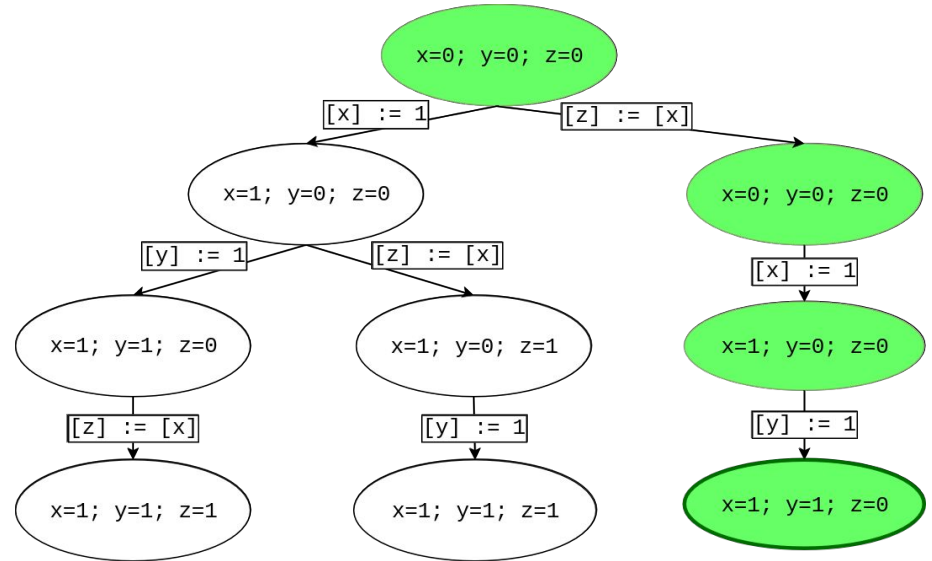
Exists output s.t. $z=0$?



Angelic Execution

Input: $x=0; y=0; z=0$

Exists output s.t. $z=0$?



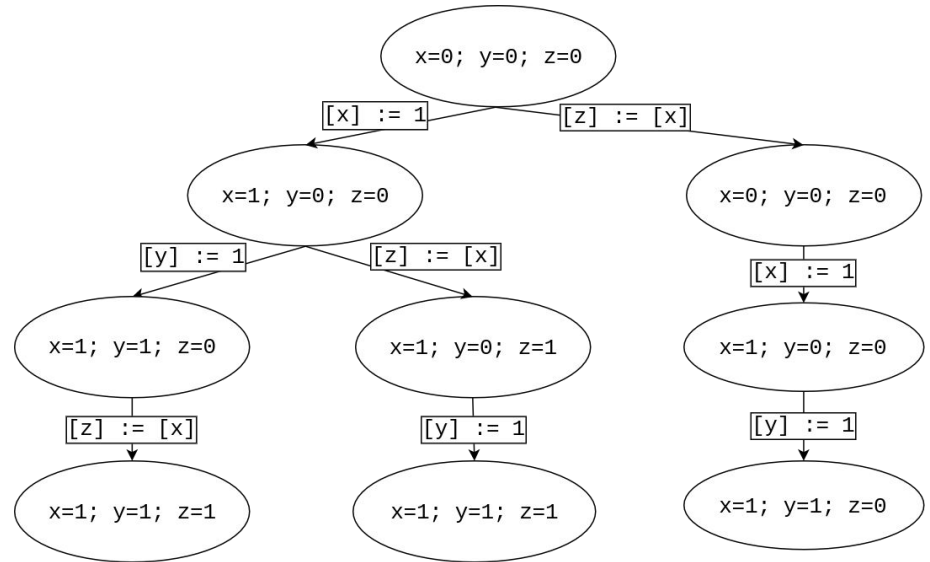
Verification

Input: $x=0; y=0; z=0$

For all outputs $z=0$?



Not Exists output s.t. $z \neq 0$?



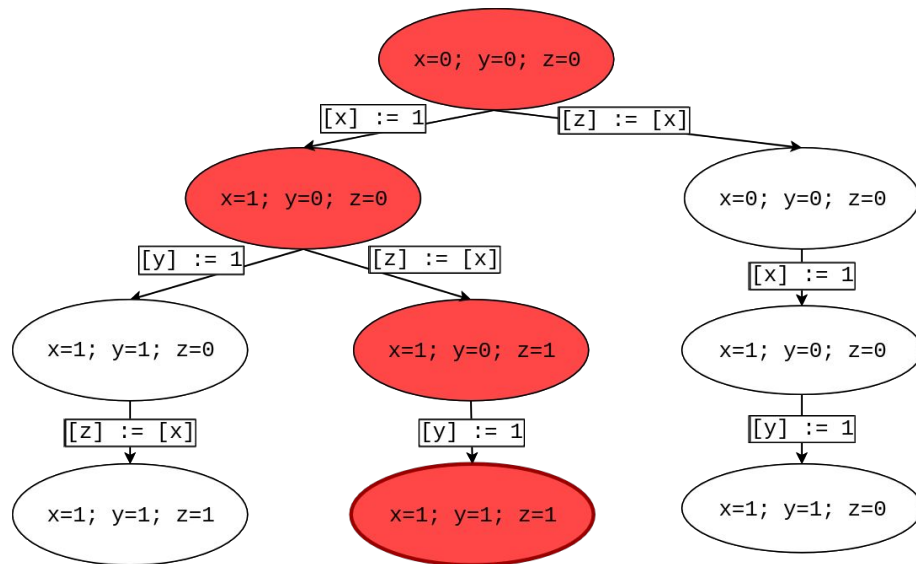
Verification

Input: $x=0; y=0; z=0$

For all outputs $z=0$?



Not Exists output s.t. $z \neq 0$?



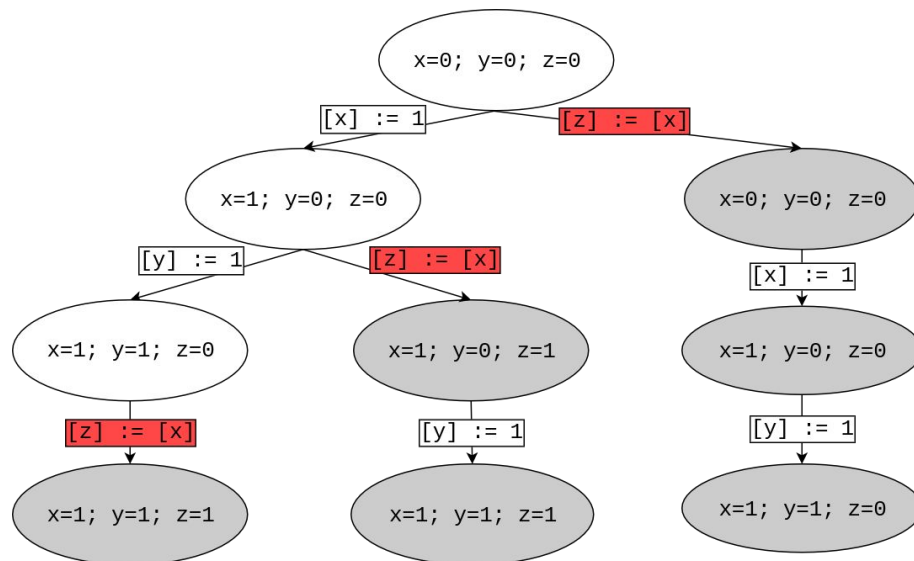
Verification

Input: $x=0; y=0; z=0$

For all outputs $z=0$?



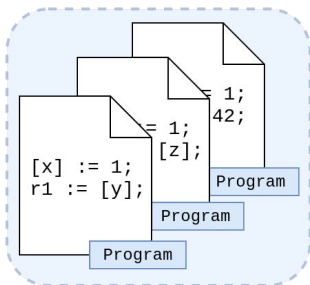
Not Exists output s.t. $z \neq 0$?



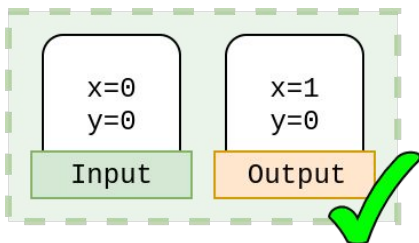
Constructive Negation

- Checks that some state is unreachable
- Otherwise provides counterexample or constraints on program
- Allows to express negative examples

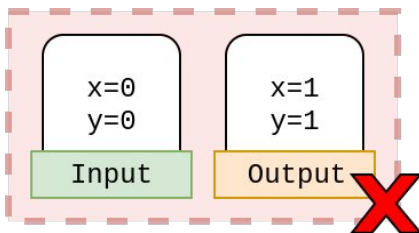
Programming By Examples



- Space of candidate programs
 - usually defined by the grammar

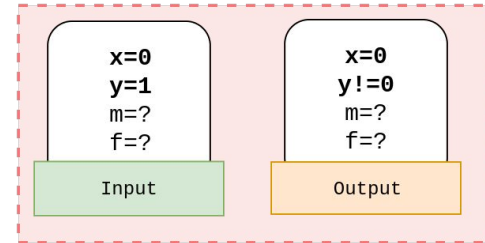
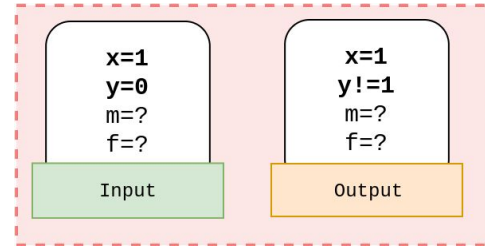
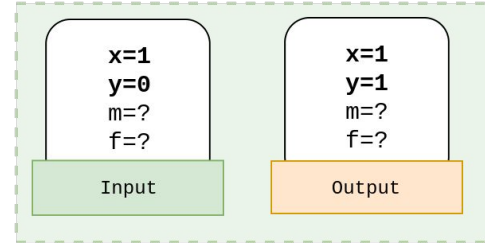
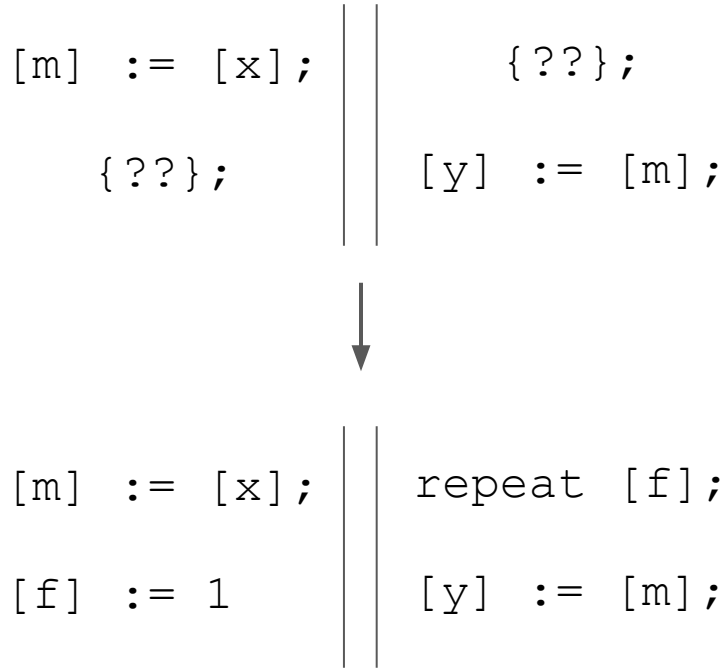


- Set of positive examples



- Set of negative examples

Programming By Examples: Message Passing



Synthesis Time

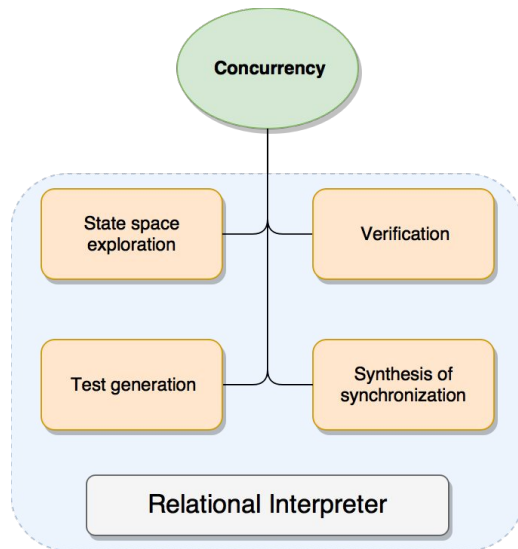
Name	#instructions	Time (s)
message passing 2 threads	4	0.39
consensus 2 threads	10	1.10
Dekker's like 2 threads	10	15.88

Limitations and Future Work

- State space explosion
 - Abstract interpretation and Abstraction refinement
- Synthesis does not scale to big programs
 - More sophisticated algorithms
 - Counterexample guided inductive synthesis

Relational Interpretation of Concurrency

- Relational Programming
 - Declarative non-deterministic computations
- Relational Interpreter
 - Framework for verification and synthesis prototyping



<https://github.com/eucpp/relcppmem>

<https://github.com/dboulytchev/OCanren>